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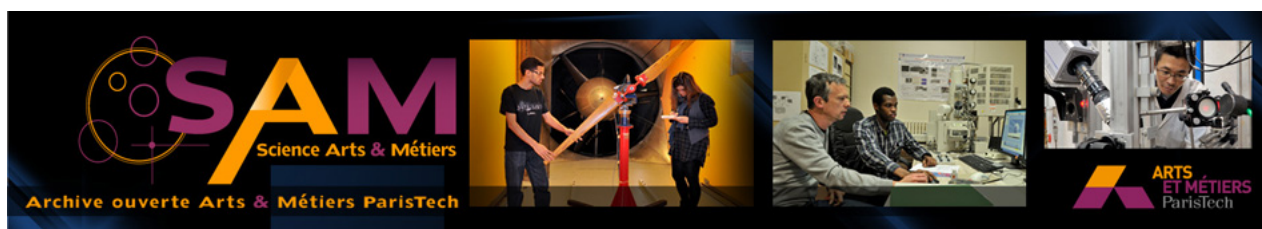
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Abstract

In this paper we report an unprecedented level of integration of self-actuated nanoelectromechanical system (NEMS) resonators based on a 150 nm thick lead zirconate titanate (PZT) thin film at the wafer-scale. A top-down approach combining ultraviolet (UV) lithography with other standard planar processing technologies allows us to achieve high-throughput manufacturing. Multilayer stack cantilevers with different geometries have been implemented with measured fundamental resonant frequencies in the megahertz range and Q-factor values ranging from ~130 in air up to ~900 in a vacuum at room temperature. A refined finite element model taking into account the exact configuration of the piezoelectric stack is proposed and demonstrates the importance of considering the dependence of the beam's cross-section upon the axial coordinate. We extensively investigate both experimentally and theoretically the transduction efficiency of the implemented piezoelectric layer and report for the first time at this integration level a piezoelectric constant of $d_{31} = 15 \text{ fm V}^{-1}$. Finally, we discuss the current limitations to achieve piezoelectric detection.

Keywords: NEMS, PZT, large-scale integration

1. Introduction

The transition from micro to nano-scale raises a major interest for both scientific and technological communities. With advances in nanotechnology the realm of electromechanical systems has witnessed the emergence of nanoelectromechanical systems (NEMS) over the last decade. The significant

enhancement of devices' performance when scaling down the size has been widely reported for NEMS-based resonators [1–3]. Characteristics such as high resonant frequencies (MHz–GHz range), low masses and high quality factors have led to unprecedented sensitivities to extremely small forces and additional mass loading. In recent years, new records for the limit of detection (i.e. the minimum resolvable added

mass) have been continuously established [4–6] until the ultimate mass-sensing limit in the yoctogram range (10^{-24} g) was recently achieved by Bachtold and co-workers [7]. These attributes make NEMS resonators particularly promising candidates for a wide range of technological applications such as biosensing [8, 9] and mass spectrometry [7, 10] as well as more fundamental studies on quantum phenomena [11, 12].

However, most of the tremendous demonstrations reported here have been obtained with individually fabricated NEMS based on external transducers (i.e. off-chip) for which actuation and read-out means typically exceed the size of the device itself. These barriers currently limit their widespread use as cheap portable sensing tools. In order to exploit the full potential of NEMS and to start being a viable alternative to their microscale counterparts (i.e. MEMS), the fully integrated transduction (i.e. on-chip) combined with large-scale integration are the ultimate goals to achieve. So far, minimal effort has been focused on the development of nanoresonators with on-chip transducers at the wafer-scale. As the size of the mechanical element is scaled downward so is its motional range and developing suitable transduction techniques of sub-nanometer displacements at high frequencies remains an important technological challenge [13]. Relevant results in that sense have been obtained mostly at the chip level either by carrying over traditional transduction schemes at the nano-scale from the MEMS domain [14–16] or by delivering brand new schemes exclusively adapted to the NEMS realm [17]. Recent efforts have been made to demonstrate full-wafer fabricated NEMS with integrated transduction means [18, 19] but these are rather infrequent, which demonstrates how critical the gap between chip and wafer is.

Compared to most of the conventionally-employed magnetomotive [20], electrostatic [14] and electrothermal [4, 21] excitations for which the integration potential may be limited by either the need for an external magnetic source, low actuation efficiency or high power consumption, piezoelectric transducers scale attractively to the sub-micron range. Such transducers offer fully-integrated transduction mechanisms to convert an electrical signal into a mechanical motion and vice versa. If the converse piezoelectric effect (strain upon application of an electric field) can be used as an actuator, the direct piezoelectric effect (generation of charges under an applied stress) can be employed for sensing. However, implementing such transducers with preserved piezoelectric properties at the nano-scale remains challenging.

In this paper we report an unprecedented level of integration of piezoelectrically self-actuated NEMS resonators at the wafer-scale. We use PZT as piezoelectric material mainly because of its excellent actuation properties compared to other ceramics [22, 23] even when geometrically constrained at extreme scale [24]. This study is part of a comprehensive approach that addresses the design, fabrication, modeling and characterization of these devices. The objectives of the paper are (i) to report a fabrication process to integrate at the wafer-scale a 150 nm thick sputtered PZT thin film onto arrays of NEMS resonators; (ii) to experimentally investigate the mechanical dynamical behavior of the fabricated resonators

and (iii) to assess the actuation and sensing capabilities of the integrated piezoelectric layer.

The outline of the paper is as follows. A detailed description of the beams' geometries and the implemented fabrication process is presented in section 2. Then a refined finite element (FE) model taking into account the complex laminated configuration of the piezoelectric stack is proposed in section 3. Finally, the characterization results are gathered and analyzed in section 4: first, the experimental resonant frequencies of several resonators are compared to the theoretical ones, validating the FE model and assessing the mechanical integrity of the resonators; then, the piezoelectric actuation and detection capabilities of the piezoelectric layer are identified and analyzed.

2. Experiments

2.1. Design

Chips (16×16 mm) of 256 silicon-based cantilevers have been designed to be fabricated on a 4 inch silicon-on-insulator (SOI) wafer. Resonators with different sizes and geometries have been implemented into 64 arrays of 4 cantilevers. The width of the cantilevers has been varied from 0.7 to $5 \mu\text{m}$ in width and from 2 to $12 \mu\text{m}$ in length. A multilayer stack composed of a 150 nm thick PZT 54/46 ($\text{PbZr}_{0.54}\text{Ti}_{0.46}\text{O}_3$) thin film sandwiched between a 100 nm thick lanthanum nickelate (LaNiO_3 or LNO) bottom electrode and a 12/120 nm thick titanium/platinum (Ti/Pt) top electrode serves as the integrated piezoelectric transducer. Two different geometries for the piezoelectric stack have been implemented. In geometry A, the piezoelectric stack covers almost the full length of the resonator and each layer of the stack is completely covered by the upper layer. In geometry B, half-length of the cantilever is covered by the piezoelectric stack for which both the bottom and top electrodes have the same dimensions. The four cantilevers of the same array have the same width and geometry but different lengths.

2.2. Fabrication process

Resonators have been fabricated by using standard surface micromachining techniques. We chose ultraviolet (UV) lithography as a parallel top-down approach to simultaneously manufacture a high number of devices with small features size in an integrated fashion at the wafer-scale. UV stepper photo-repeater equipment was used (I-line FPA 3000 i4/i5 N A 0.63, Canon Inc) to perform the photolithography steps during the fabrication process. The I-line photolithography (of wavelength $\lambda = 365$ nm) combined with an X5 (lens reduction factor) projection system allows us to reach a resolution of 350 nm for a periodic pattern and up to 100 nm for an isolated structure with a precision alignment of 50 nm. We used 4 inch (100) P-type silicon on insulator (SOI) wafers (340 nm thick device layer / $1 \mu\text{m}$ thick buried oxide / $525 \mu\text{m}$ thick handle, purchased from Soitec Inc, France) as the starting material. The buried oxide acted as a sacrificial layer for the final release of the structures. The main steps of the six-mask fabrication process are shown in figure 1 and described in the following.

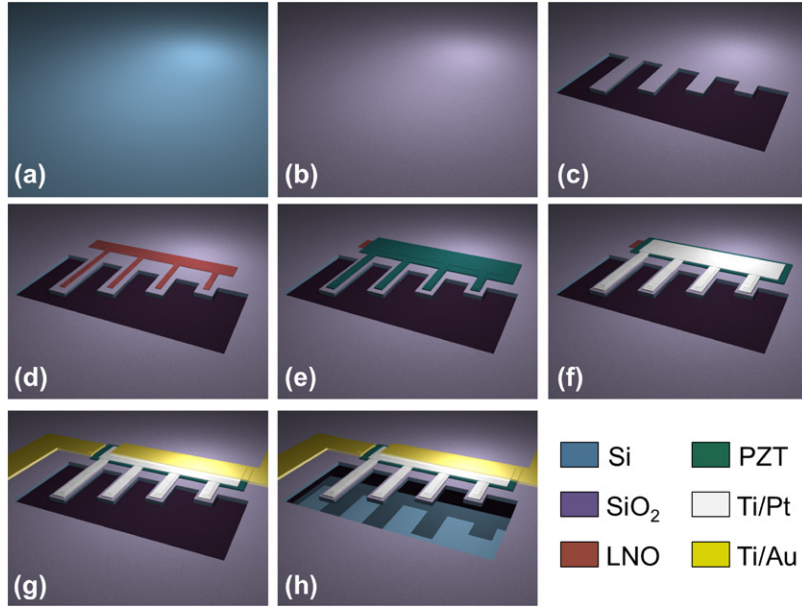


Figure 1. Process flow for the cantilevers' fabrication (geometry A) with an integrated PZT-based piezoelectric transducer. (a) 4-inch SOI wafer (340 nm thick top Si layer, 1 μm -thick buried oxide) as the starting material. (b) Dry thermal growth of 30 nm thick silicon dioxide (SiO_2). (c) Definition of the shape of the cantilevers by reactive ion etching (RIE). (d) Deposition and lift-off patterning of a 100 nm thick LNO bottom electrode. (e) Deposition by RF-magnetron sputtering and lift-off patterning of a 150 nm thick PZT active layer. (f) Deposition and lift-off patterning of a 12/120 nm thick Ti/Pt top electrode. (g) Metallization and lift-off patterning of 100/700 nm thick Ti/Au interconnections. (h) Devices released by two subsequent anisotropic wet etchings of the sacrificial buried SiO_2 layer. The color code used is the same as for figures 1, 2 and 4.

First, a 30 nm thick layer of SiO_2 is thermally grown to serve as an electrical insulation layer. Both thermal oxide (CF_4 : 40 sccm, RF power: 39 W, ICP power: 500 W, etching time: 35 s) and silicon device (C_4F_8 : 400 sccm, SF_6 : 300 sccm, RF power: 60 W, ICP power: 2800 W, pressure: 0.07 mbar, sample temperature: -5°C , etching time: 20 s) layers are then successively etched by reactive ion etching (AMS4200, Alcatel Inc) to pattern the shape of the structures. Collective integration of the piezoelectric stack onto individual structures starts with the deposition of the bottom electrode. A 100 nm thick layer of LaNiO_3 is sputtered [24] and patterned on the structures by lift-off using a high-resolution bi-layer positive photoresist LOR3A/ECI3012 (purchased from MicroChemicals, Germany). LNO acts as a diffusion barrier against the migration of lead atoms during the PZT crystallization step. It prevents lead atoms from diffusing and reacting with any underlying Si-based material. Then a 150 nm thick active layer of PZT 54/46 is deposited by RF magnetron sputtering (Addax Technologies) from a $\text{PbZr}_{54}\text{Ti}_{46}\text{O}_3$ compact power target (diameter 76.2 mm) under a pure argon gas atmosphere with a pressure set at 0.01 mbar and with a RF power fixed at 100 W [24]. The deposition is performed at room temperature to be compatible with a lift-off patterning. The PZT composition is close to the morphotropic phase boundary (MPB) where PZT exhibits optimal piezoelectric and dielectric properties [25]. PZT patterning by lift-off is an alternative approach to conventional dry and wet etching techniques. The former has been reported to deteriorate the PZT material properties due to a combination of both physical damages and chemical contamination [26, 27] while the latter requires the use of a hydrofluoric (HF) solution which can be incompatible with other etchant-sensitive materials and suffers

from undesirable undercut of the masked features. After deposition, a mandatory annealing at 625°C for 30 min is performed to crystallize the PZT into the perovskite phase. A 12/120 nm thick layer of Ti/Pt is then deposited and patterned by lift-off as the top electrode. Each array of structures is then individually addressed with 100/700 nm thick Ti /Au interconnections. The structures are released by wet etching of the sacrificial layer after a photoresist encapsulation to protect other sensitive layers. We use a 2.6 μm thick ECI 3012 positive photoresist (purchased from MicroChemicals, Germany) with an additional baking at 115°C for 1 min before etching to enhance the photoresist adhesion. A buffered oxide etchant (BOE) composed of a 7-1 ratio of an ammonium fluoride (NH_4F)–HF acid mixture with an isotropic etch rate of around 77 nm min^{-1} is used at room temperature to release the structures. Two subsequent wet etching-photoresist encapsulations are performed to reduce photoresist adhesion defects due to long etching time while being able to release the largest structures up to $5 \mu\text{m}$ wide. Nevertheless, this critical step imposes the final yield (around 33%) of the implemented fabrication process. Optical and SEM pictures of the fabricated devices are shown in figure 2.

2.3. Measurement setup

Actuation of the resonators is performed according to two different configurations: external actuation (off-chip) and integrated actuation (on-chip). In the former, a chip is mounted onto a piezodisk electrically driven by a network analyzer, as shown in figure 3(a). Resonators are therefore collectively actuated through the piezoshaker and individually read-out. In the latter configuration, a chip is glued to a metallized

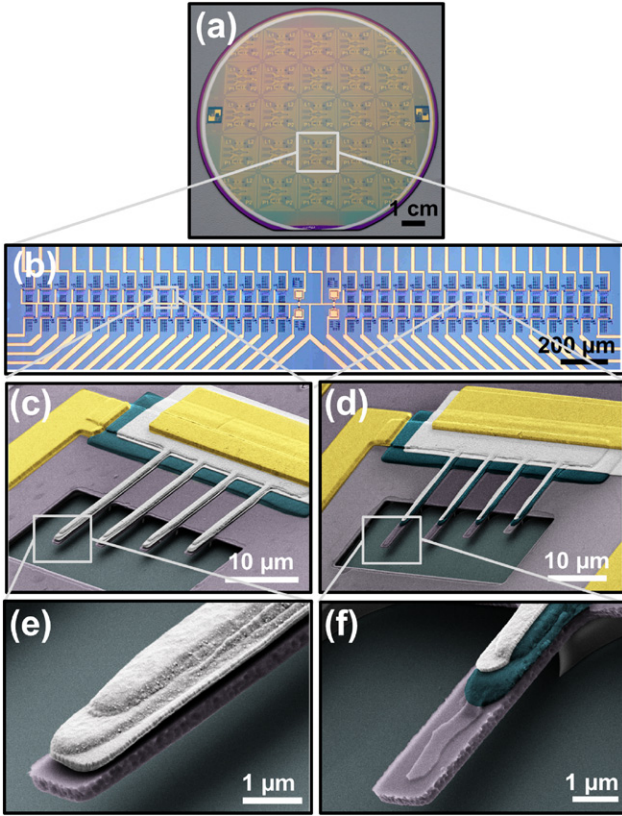


Figure 2. (a) Wafer-scale fabrication of NEMS cantilevers on a 4 inch SOI wafer. (b) Each chip is composed of 64 arrays of 4 cantilevers. Colored scanning electron microscope (SEM) pictures of 2 arrays of $2.4\mu\text{m}$ wide cantilevers with geometries A and B are respectively shown in (c) and (d). A close view of the two configurations for the multilayer stack is shown in (e) and (f).

polyimide support with dedicated gold-wiring interconnections. Devices of the same array are then self-actuated by imposing a voltage between the top and bottom electrodes with the network analyzer (see figure 3(b)).

For both actuation configurations, the mechanical motion of individual cantilevers is optically read-out by a home-made Fabry–Pérot interferometer bench shown in figure 3(c). In this setup, a chip is clamped onto a motorized piezoelectric precision stage (XYZ translations) inside a vacuum chamber and pumped down to a secondary vacuum (around 10^{-6} mbar) at room temperature. A 30 mW helium-neon laser (of wavelength $\lambda = 633$ nm) is focused through a beam expander (X5) and a long-working distance microscope objective (20X, N A 0.28) onto the surface of a resonator. The fine positioning of the laser is controlled by the piezo-stage displacement while the operation is monitored with a complementary metal oxide semiconductor (CMOS) camera under a light emitting diode blue light (of wavelength $\lambda = 470$ nm). The air gap between the suspended resonator and the substrate underneath acts as a Fabry–Pérot cavity. Mechanical oscillations of the driven resonator modify the gap size of the optical cavity and modulate the intensity of the interferences between the multiple reflected beams. The intensity of the reflected optical signal is modulated at the driving frequency and its amplitude is proportional to the resonator displacement. Details of the

Fabry–Pérot interferometry principle used as a sensing technique for MEMS have been described by Carr and Craighead [28]. The optical signal is reflected back through the microscope objective and diverted through a beam splitter toward an ac-coupled photodetector (New Focus model 1601, Newport Inc). The photodetector ac output is connected to the network analyzer (Agilent model 4395A) to measure the mechanical response of the resonator at the frequency of the excitation signal, in a similar manner to a lock-in amplifier detection.

3. Model for laminated resonating cantilevers

A reduced-order model of the vibrating cantilevers, restricted to one eigenmode, is proposed hereafter. We are interested in the tip transverse displacement $u_t(t)$ (at time t). It can be shown (see appendix A) that it verifies:

$$\ddot{u}_t + Q^{-1}\omega_0\dot{u}_t + \omega_0^2 u_t + \chi_c V = \frac{p_0 L}{M_{\text{eff}}}, M_{\text{eff}} = \frac{L \int_0^L m(x) \Phi^2(x) dx}{\Phi(L) \int_0^L \Phi(x) dx} \quad (1)$$

where Q is the quality factor, ω_0 is the angular frequency, χ_c is the modal converse piezoelectric-coupling coefficient, $V(t)$ is the voltage across the electrodes, L is the length of the cantilever, $m(x)$ is the cantilever mass per unit of length and $\Phi(x)$ is the mode shape at axial position x . Only a uniform mechanical loading p_0 (a force per unit of length) of the cantilevers is considered here (it will be associated with the thermomechanical noise in section 4.2). M_{eff} is the effective mass, which depends on the detection location (the free end) and the type of loading (uniform in this case). Equation (1) is associated with the converse piezoelectric effect.

For the direct piezoelectric effect, one obtains [29, 30] the electric charge q in the electrodes as:

$$q = CV + \chi_d u_t \quad (2)$$

where C is the static capacitance of the piezoelectric layer and χ_d is the modal direct piezoelectric-coupling coefficient. In this latter equation, one clearly observes two physical effects that generate electric charges in the electrodes: (i) a capacitive effect CV , directly proportional to the input voltage V and (ii) a direct piezoelectric transduction effect $\chi_d u_t$.

As explained in section 2.1, the geometries of the cantilevers are not homogeneous since they are composed of several materials, resulting in a complex layered structure which depends on the axial coordinate (see figure 4).

In the current study, a home-made finite element (FE) model, fully described elsewhere [29–31], enables us to compute all the model parameters (ω_0 , $\Phi(x)$, M_{eff} , χ_c and χ_d). It is based on 1D beam finite elements, with Euler–Bernoulli assumptions and a uniform electric field inside the piezoelectric layer. 100 finite elements are used in the model, which enables us to accurately take into account the dependence of the lamination as a function of the axial coordinate, by changing the value of the equivalent mass and stiffness properties of the elements. Four types (resp. three types) of cross-sections for cantilevers

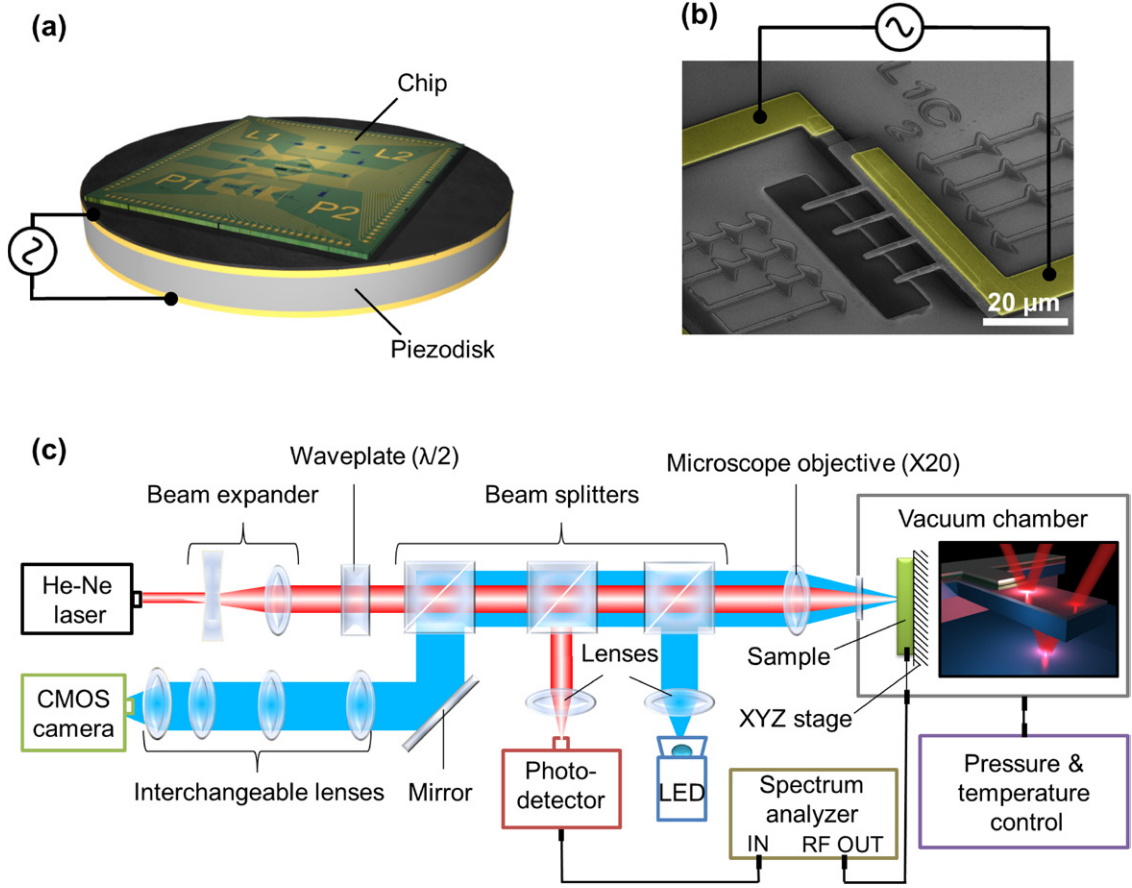


Figure 3. Scheme of the entire measurement setup. The two actuation configurations external (off-chip) and integrated (on-chip) are respectively shown in (a) and (b). The optical interferometry setup is depicted in (c).

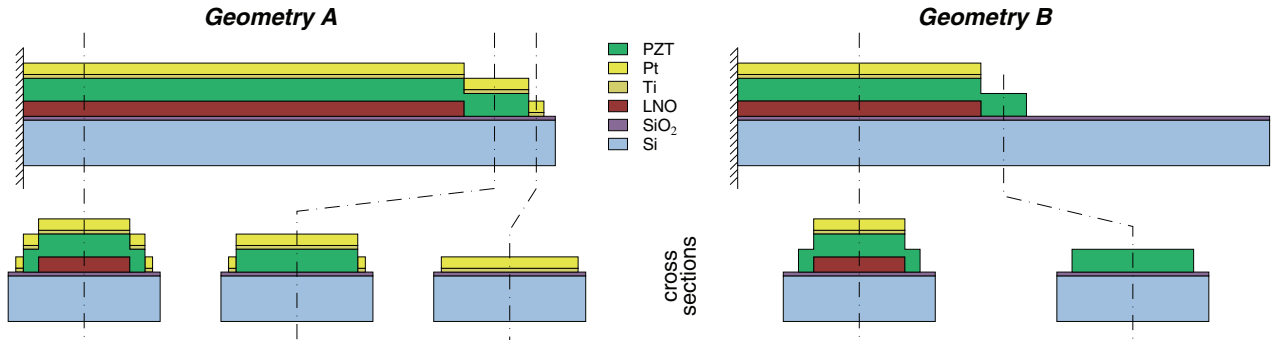


Figure 4. Geometries of the beams used in the finite element simulations.

with geometry A (resp. geometry B) are defined, whereas other works in the literature based on analytical models are limited to only one cross section [32, 33] or two [30]. Table 1 gathers the parameters used for the computations.

4. Results and discussion

The fabricated resonators are characterized in their dynamic mode. For each measurement, the dynamic parameters such as the resonant frequency f_0 and the quality factor Q are extracted from the mechanical response by a Lorentzian curve fitting based on the least squares method. Table 2 gathers

Table 1. Values of the numerical parameters used for the FE simulations. The Young's moduli values are from [34] (Si, SiO₂, PZT, Pt [35]), (LNO) and [36] (Ti). The density values are the common ones from equivalent bulk materials.

Material	Thickness [nm]	Density [kg m ⁻³]	Young's modulus [GPa]
Si	340	2500	169
SiO ₂	30	2150	70
LNO	100	7215	180
PZT	150	7800	96
Ti	12	4510	110
Pt	120	21450	145

Table 2. Dimensions and geometries of the stratified cantilevers studied in this work.

Cantilever	Length L [μm]	Width w [μm]	Geometry
C1	10.3	2.4	A
C2	8.3	2.4	A
C3	6.3	2.4	A
C4	10.15	1.6	B
C5	10.2	1.8	B
C6	8.15	1.6	B
C7	8.2	1.8	B
C8	10.2	2	B
C9	8.2	2	B

the dimensions and geometries of the different cantilevers reported in this work.

In addition to the dynamic and piezoelectric responses of the fabricated resonators reported in the following section, experimental characterizations of other major attributes for mass-sensing applications, such as the Q -factor dependence with air pressure and the added-mass limit of detection ($5 \text{ ag } \mu\text{m}^{-2}$), are available as supplementary data (stacks.iop.org/JMM/25/035002/mmedia).

4.1. Model validation

A first characterization of the cantilevers is performed in a vacuum at room temperature, according to the external transduction configuration (see figure 3(a)). Cantilevers are collectively actuated by applying an ac voltage to the piezoelectric disk and individually read-out with the Fabry–Pérot setup (see figure 3(c)).

Values of the fundamental resonant mode measured for the cantilevers are plotted on figure 5(a). They are compared to theoretical values obtained by the FE model described in section 3, which takes into account the exact geometries and configurations of the piezoelectric stack. Figure 5(a) shows that a very good agreement is obtained, since all the measured points are located around the $y = x$ line. The agreement is excellent (from 0.2% to 2.5%) for cantilevers with geometry A (C1, C2, C3), whereas it is not as good for cantilevers with geometry B (C4 to C9, from 1 to 16%). Figure 5(a) also shows the comparison between the experimental results and the natural frequencies obtained from a classical analytical model (see [32, 33] among others) applied to a cantilever beam with a uniform cross section along the axial coordinate (homogeneous stack). Two configurations are considered for this latter analytical model: a 2-layer stack composed of only the first two layers of Si and SiO_2 (the piezoelectric stack being neglected) and a 6-layer stack (with a homogeneous piezoelectric stack covering the whole length and width of the beam). The obtained points are far from the $y = x$ line since they are related to discrepancies between 12% and 54%.

Figure 5(b) shows the mode shape of the first mode of a cantilever with geometry A, computed with the FE model and with a homogeneous beam model. The mechanical (mass and stiffness) influence of the piezoelectric stack on the elasticity of the beam is clearly noticeable.

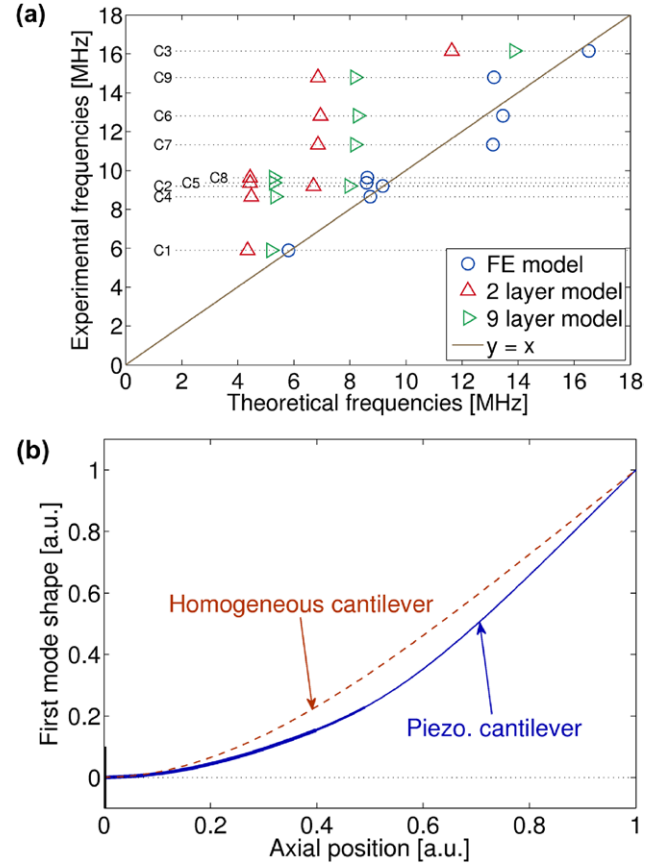


Figure 5. (a) Experimental natural frequencies as a function of the theoretical ones for the first mode of cantilevers C1 to C9. Results from the refined FE model (blue circle symbols) are compared to a classical analytical model of a cantilever beam with a uniform cross section composed of the first two layers Si and SiO_2 (red triangle symbols) and composed of the whole stack (green triangle symbols). The first bisector $y = x$ (solid brown line) is represented to visualize the discrepancies between the measurements and the predictions. (b) Comparison of the first mode shape between a homogeneous cantilever (dashed line) and a laminated cantilever beam with geometry B (solid line). The thickness of the line is proportional to the thickness of the cantilever.

In conclusion, these results show that the influence of both the mass and stiffness of the piezoelectric stack on the elasticity of the beam cannot be neglected and that the dependence of the beam's cross-section upon the axial coordinate has to be taken into account. Those features are correctly captured by the refined FE model. It must be noted that the inherent undercut due to the wet etching release was not taken into account in the FE modeling. Its influence for single layer cantilevers has been studied elsewhere [37] and is probably negligible compared to the one of the piezoelectric stack for the current piezoelectric beams. Finally, the good agreement between theory and experiment demonstrates the preserved mechanical integrity of the structures after fabrication.

4.2. Thermomechanical noise as a calibration tool

Thermomechanical fluctuations arise from the thermal coupling of a resonator with its environment at a nonzero

temperature. They result in the random displacement of the resonator around its equilibrium position in response to a time randomly fluctuating force. The thermomechanical force noise $F_{th}(t)$ is commonly characterized by its power spectral density (PSD) $S_{F,th}$ defined as the Fourier transform of its autocorrelation function. The PSD ($N^2 Hz^{-1}$) associated with the force noise has a white spectrum and its expression can be obtained from the fluctuation-dissipation theorem:

$$S_{F,th} = 4k_B T c = \frac{4k_B T M_{eff} \omega_0}{Q} \quad (3)$$

where M_{eff} is the equivalent mass of the resonator, Q is the quality factor, $\omega_0 = 2\pi f_0$ is the fundamental angular frequency ($rad s^{-1}$), c is the damping coefficient defined as $c = M_{eff} \omega_0 / Q$ in the one degree of freedom harmonic oscillator equivalent model of the resonator, k_B is the Boltzmann constant and T is the temperature.

In the frequency domain, the PSD related to the random displacement $S_{U,th}(f)$ ($m^2 Hz^{-1}$) is connected to the PSD of the fluctuating force noise $S_{F,th}$ by the transfer function $H(f)$ of the resonator according to [38]:

$$S_{U,th}(f) = |H(f)|^2 S_{F,th} = \frac{S_{F,th}}{16\pi^4 M_{eff}^2 \left[(f^2 - f_0^2)^2 - \frac{f^2 f_0^2}{Q^2} \right]} \quad (4)$$

The thermomechanical displacement at resonance is therefore obtained for $f = f_0$:

$$S_{U,th}(f_0) = \frac{k_B T Q}{M_{eff} 2\pi^3 f_0^3} \quad (5)$$

Assuming an implementation with low-noise electronics, the thermomechanical noise sets the intrinsic and fundamental limit of detection for dynamic resonators. Roukes and co-workers reported an elegant way to use the thermomechanical noise as a calibration tool for the response of their optical read-out scheme [15]. The same method is followed here.

Our Fabry-Pérot measurement setup is sufficiently sensitive to detect the thermomechanical fluctuations of cantilevers in a vacuum (1.1×10^{-6} mbar) at room temperature ($23^\circ C$). The voltage spectral density $S_{V,th}^{1/2}(f)$ (V/\sqrt{Hz}) related to the displacement of a cantilever with geometry C4 is plotted in figure 6(a) and is obtained from the square root of the measured PSD. The spectrum has a background noise floor of $S_{V,background}^{1/2}(f) \approx 1.745 \mu V/\sqrt{Hz}$ near resonance due to the presence of other noise sources (laser, photodiode, spectrum analyzer). Since the noise sources are uncorrelated, the total measured PSD is the sum of the contributions of each individual noise source: $S_V = S_{V,th} + S_{V,background}$. The voltage noise spectral density related to thermomechanical fluctuations can therefore be resolved by subtracting the contribution from the noise background according to: $S_{V,th}^{1/2} = (S_V - S_{V,background})^{1/2} \approx 1.694 \mu V/\sqrt{Hz}$. A Lorentzian fit allows us to determine both the resonant frequency $f_0 \approx 8.656$ MHz and the quality factor $Q \approx 296$. The effective mass is computed according to the FE model (cf. equation (1)) for a cantilever vibrating in the fundamental flexural mode, under a uniform mechanical loading

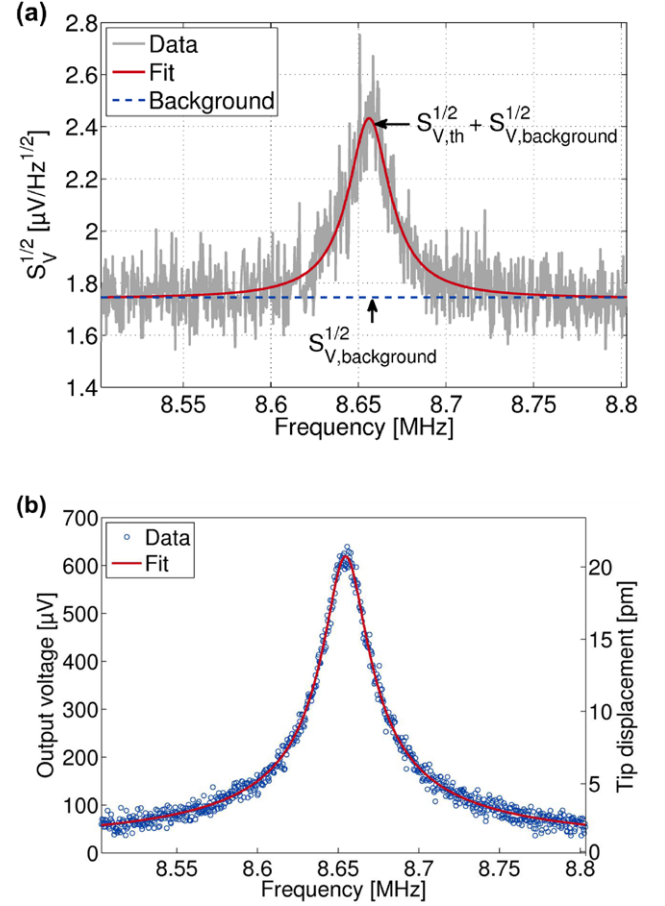


Figure 6. (a) Measurement in a vacuum (1.1×10^{-6} mbar) at room temperature ($23^\circ C$) of the total voltage spectral density $S_V^{1/2}$ of a cantilever with geometry C4 due to the thermomechanical noise (blue circle symbols) and its Lorentzian fit (red solid line). (b) Fundamental resonant response (blue circle symbols) obtained for the cantilever C4 by imposing a driving voltage between the top and bottom electrodes with an amplitude of 156 mV and its Lorentzian fit (red solid line).

($F_{th} = Lp_0$), a zero external voltage ($V = 0$) and a displacement measured at the tip (free end). The FE simulations give: $M_{eff} = 0.31226 \times M \approx 9.36$ pg, with M the total mass of the cantilever. Equation (5) yields to: $S_{U,th}^{1/2}(f_0) \approx 0.06$ pm/ \sqrt{Hz} at room temperature. The optical transduction responsivity defined as the conversion coefficient of the photodetector output voltage into the resonator's mechanical displacement is finally obtained: $R = S_{V,th}^{1/2} / S_{U,th}^{1/2} \approx 30 \mu V pm^{-1}$.

This calibration technique is quite straight forward since it only depends on the cantilever's dynamic properties, assuming the optical setup is sensitive enough to detect the thermomechanical motion. However, one has to keep in mind the possible uncertainty sources. First, the calculation requires the effective mass of the cantilever which is experimentally unknown and which is here computed with the FE model for a displacement measured at the end of the beam. Secondly, the positioning accuracy of the laser spot exactly at the cantilever's tip during the experiment may also affect the calculation. However, we believe that a fair estimation of the range of the mechanical displacement is obtained.

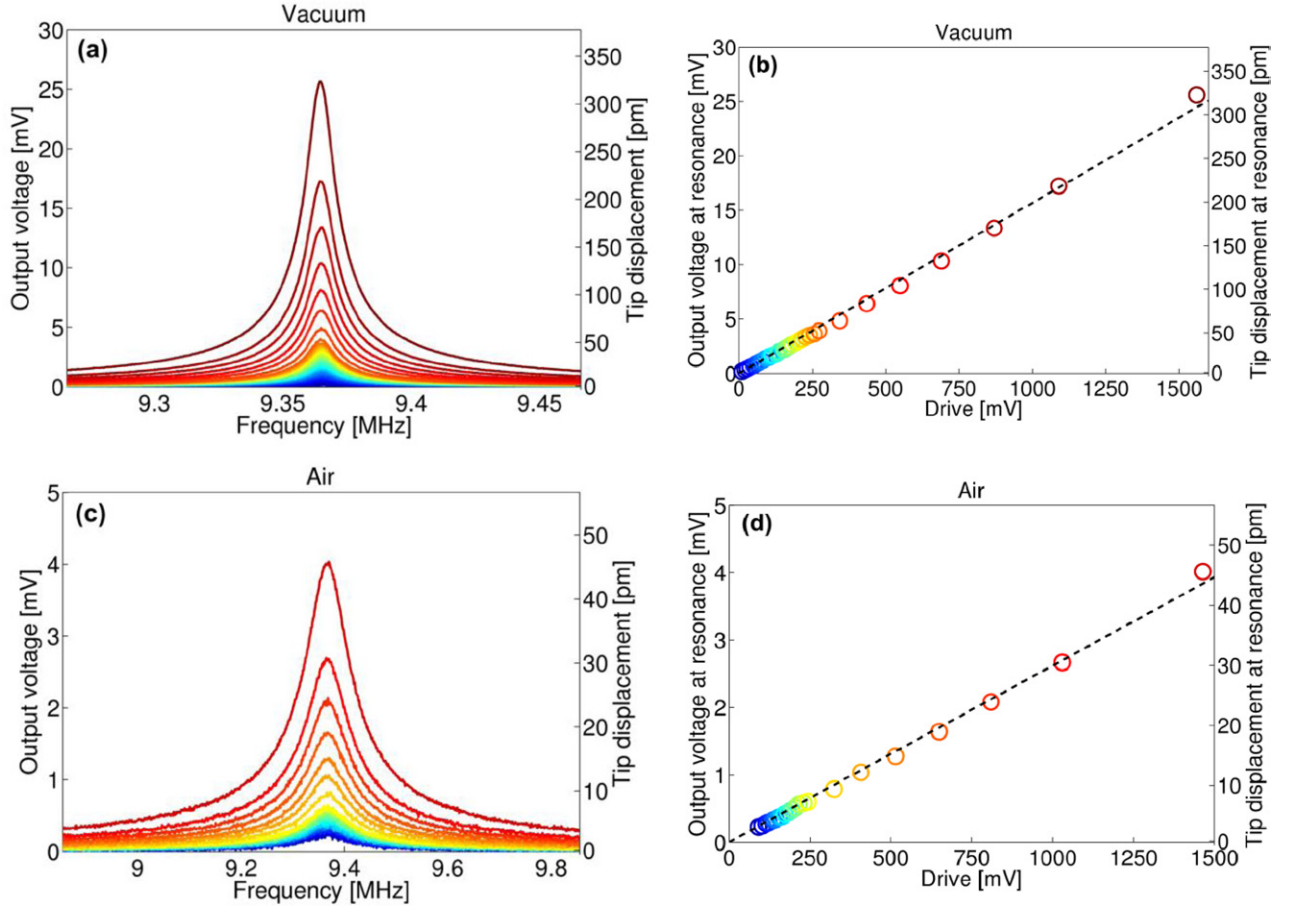


Figure 7. Resonant spectra of a cantilever with geometry C5 under a range of driving voltages measured in a vacuum (a) and in air (c) environments. The amplitude of the tip displacement at resonance in vacuum (b) and in air (d) varies linearly with the driving voltage. The slope of the linear fit corresponds to the piezoelectric response coefficient η .

4.3. Assessment of the piezoelectric actuation

In this configuration, devices are self-actuated by imposing a voltage between the top and bottom electrodes (see figure 3(b)) while the mechanical motion is optically read-out with the Fabry-Pérot setup (see figure 3(c)). Due to the converse piezoelectric effect, the transverse electric field resulting from the applied voltage causes a longitudinal strain in the PZT thin film. Since the piezoelectric layer is offset from the neutral axis of the resonator, the strain causes a bending moment in the cantilever. The active layer elongates and contracts at the frequency of the excitation voltage, thereby driving the cantilever in oscillations at the driving frequency. A typical resonant response measured in a vacuum for a cantilever with geometry C4 under a driving amplitude of 156 mV is shown in figure 6(b). The transduction responsivity calculated in section 4.2 can be used to convert the photodetector output voltage into an estimated mechanical displacement of the tip of around 20 pm at resonance.

The resonator's dynamic with in the linear regime was also investigated by varying the ac driving voltage. Resonant peaks of a cantilever with geometry C5 were measured over almost two orders of magnitude of driving voltage at room temperature in a vacuum, as well as atmospheric pressure (see figure 7). The resonant frequency for the fundamental mode is found constant over the entire range of driving voltage (≈ 23 ppm variation), and with a variation of the Q-factor of

around 3%. For both vacuum and air environments the peak amplitude at resonance varies linearly with a constant dissipation confirming that the resonator operates in the linear regime. The Q-factor is found to drop by a factor of 7 during the transition from vacuum to air but remains sufficiently high to be easily measured.

The photodetector output voltage is converted into a mechanical displacement by using the calibration technique as explained in section 4.2. The actuation efficiency of the piezoelectric layer for this cantilever in a vacuum can then be characterized by the coefficient η , defined as the slope of the linear curve shown in figure 7(b). A tip displacement of $\eta = u_t / V \approx 181 \text{ fm mV}^{-1}$ at resonance is obtained for a cantilever with geometry C5. This constant can be related to the modal converse piezoelectric-coupling coefficient χ_c (consider equation (1) in resonant harmonic piezoelectric driving):

$$\eta = \frac{\chi_c Q}{\omega_0^2} \quad (6)$$

Since χ_c is proportional to the piezoelectric material constant d_{31} , computing χ_c with the FE code of section 3 (which takes into account the theoretical laminated geometry of the piezoelectric stack), leads us to estimate an experimental value of $d_{31} = 1.89 \text{ fm V}^{-1}$ for a cantilever with geometry C5.

Table 3. Data obtained from both the FE model and measurements for 6 cantilevers with the same geometry B but with different dimensions. Measurements performed in a vacuum and in air are shown. f_0 is the resonance of the fundamental mode, M is the total mass of the cantilever, M_{eff}/M is the dimensionless effective mass with a uniform mechanical loading, R is the optical responsivity, Q is the quality factor, σ is the standard deviation, η is the actuation efficiency of the piezoelectric layer, χ_c is the modal converse piezoelectric-coupling coefficient, d_{31} is the piezoelectric constant, χ_d is the modal direct piezoelectric-coupling coefficient and α is the detection efficiency of the piezoelectric layer.

		C8	C9	C5	C7	C4	C6
Model	$f_{0, \text{model}}$ [MHz]	8.62	13.14	8.6	13.11	8.73	13.46
	M [pg]	37.745	29.668	33.51	26.368	29.976	23.757
	M_{eff}/M	0.31012	0.31583	0.31433	0.31976	0.31226	0.31564
Noise	R [$\mu\text{V pm}^{-1}$]	84.388	61.108	79.419	37.656	29.876	37.218
Vacuum	$f_{0, \text{vac}}$ [MHz]	9.631471	14.783769	9.365327	11.329327	8.654284	12.812904
	($\pm \sigma$) [Hz]	(± 108)	(± 244)	(± 221)	(± 221)	(± 681)	(± 1087)
	Q_{vac}	923	891	883	845	321	372
	($\pm \sigma$)	(± 14)	(± 16)	(± 28)	(± 9)	(± 5)	(± 3)
	η_{vac} [pm mV^{-1}]	6.6131	0.0481	0.1808	0.6571	0.1417	0.1488
	χ_c [$\text{m (V.s}^2)^{-1}$]	26232	465	709	3940	1307	2593
	d_{31} [fm V^{-1}]	71.3	0.89	1.89	7.38	3.33	4.49
	χ_d [pC m^{-1}]	104.3	1.48	2.52	11.29	4.11	6.6
	α [zCV^{-1}]	692.7	0.07	0.46	7.55	0.58	0.99
Air	$f_{0, \text{air}}$ [MHz]	9.624355	14.774904	9.366705	11.325511	8.665	12.832841
	($\pm \sigma$) [Hz]	(± 442)	(± 1193)	(± 616)	(± 1135)	(± 1021)	(± 3783)
	Q_{air}	130	162	127	135	94	122
	($\pm \sigma$)	(± 1)	(± 6)	(± 2)	(± 1)	(± 3)	(± 2)
	η_{air} [pm mV^{-1}]	0.9875	0.0082	0.0330	0.1268	0.0379	0.0331
	χ_c [$\text{m (V.s}^2)^{-1}$]	27855	437	900	4771	1199	1767

This extensive study has been repeated in total on 6 different cantilevers to map the homogeneity and the quality of the piezoelectric thin film. The results are gathered in table 3. A maximum value of $d_{31} = 71.3 \text{ fm V}^{-1}$ was obtained for a cantilever with geometry C8. However, the piezoelectric constant is found to vary significantly among the measured cantilevers, reflecting the non-uniformity of the deposited piezoelectric thin film. The mean value calculated over the 6 cantilevers is equal to 15 fm V^{-1} , which approximately corresponds to an absolute value for the piezoelectric coefficient of: $e_{31} = Y_p d_{31} = 1.4 \text{ mC m}^{-2}$, where $Y_p = 96 \text{ GPa}$ is the theoretical value of the piezoelectric material Young's modulus. Even though this value is sufficient to perform actuation, it is around 3 orders of magnitude lower compared to the one reported elsewhere [39] for a sputtered PZT thin film in the same thickness range onto cantilevers. However, the value reported by Arndt *et al* is given for only one cantilever with in-plane dimensions significantly larger than the sizes of the resonators presented here. The lateral confinement of the piezoelectric layer may play an important part in the global response. Still, this is the first time to our knowledge that large-scale integration of a sputtered PZT-based piezoelectric transducer onto cantilevers with such confined dimensions is demonstrated.

4.4. Discussion on the piezoelectric detection

After validation of the structures' dynamic behavior and piezoelectric actuation capabilities, an electrical detection scheme was implemented to replace the external optical

detection setup. A 1 pF charge amplifier was used to detect charges generated by the resonating structure due to the direct piezoelectric effect. In order to compensate inherent parasitic effects another structure usually serves as a [32]. The reference is expected to compensate the static capacitance of the piezoelectric stack as well as the resistance and capacitance of the interconnections. In a previous study, we investigated through electrical simulations the nature and the critical impact of parasitic effects on the behavior at resonance and experimentally validated the implementation of this detection scheme for larger structures with different geometries [40]. For the NEMS resonators studied in this current work, static capacitances with typical values of $\sim 20 \text{ pF}$ have been compensated by using the same electrical scheme. However, after compensation a residual voltage of $\sim 20 \text{ mV}$ was measured at the output of the charge amplifier near the mechanical resonance. One identified source for this background level is the difference in the wiring resistance of the interconnections as well as the difference in the resistance of the PZT layer between the resonator and the reference. The former was not optimized in the design while the latter is inherent in the fabrication process. A detection sensitivity of $\sim 20 \mu\text{V}$ was achieved with a spectrum analyzer but still no resonance was observed which would suggest a charge generated by the PZT lower than 20 aC under 1 V excitation. Impedance measurements of the piezoelectric stack have shown resistances (hundreds of $\text{k}\Omega$) significantly lower than typical values (in the $\text{G}\Omega$ range) for thicker PZT thin films. Dielectric losses within the piezoelectric material could therefore be responsible for a poor coupling coefficient

due to energy dissipation into heat and the limitation of the signal-to-noise ratio.

Equation (2) leads us to estimate the direct effect of the piezoelectric layer and thus the detection efficiency of the device. Numerical values for the piezoelectric direct-coupling coefficient χ_d are obtained by numerical computations with the FE model using the estimated d_{31} values and are reported in table 3. Then, inserting equation (6) in equation (2), one obtains the following expression for the electric charge generated by the piezoelectric direct effect at resonance:

$$q = \underbrace{\frac{\chi_c \chi_d Q}{\omega_0^2}}_{\alpha} V \quad (7)$$

where the coefficient α (C/V) characterizes the detection efficiency of the piezoelectric layer. For a cantilever with geometry C8 which exhibits the highest estimated piezoelectric constant d_{31} (see table 3), the calculated charge generated by the piezoelectric direct effect yields to $q \approx 0.7$ aC under a driving amplitude of 1 V. The estimated generated charge is therefore well below the minimum resolution achievable with our detection setup. These results show how critical the transition from the micro-scale to the nano-scale is and highlight the challenge of developing integrated transducers dedicated to the NEMS realm.

5. Conclusion

Collective fabrication at the wafer-scale of self-actuated cantilever-based resonators with an integrated 150 nm thick PZT thin film has been reported. Standard surface micro-machining technologies such as UV lithography appear as a good compromise between the degree of miniaturization and high-throughput manufacturing of resonators with integrated transduction means. Dynamic mechanical characterization of the fabricated cantilevers with different geometries have shown a preserved mechanical integrity and a dynamic behavior in a fair agreement with the finite element analysis. Quality factor values of ~ 900 in a vacuum and ~ 130 in air have been obtained at room temperature for fundamental resonant responses in the megahertz range. Piezoelectric actuation capabilities were validated in the linear regime for the first time at this integration level in spite of a low piezoelectric constant probably due to the lateral confinement. Discussion on the piezoelectric sensing shows how critical the transition from the micro-scale to the nano-scale is. This work shows promise and paves the way for further research dedicated to the NEMS realm to address the challenge of the transduction integration at the nano-scale to provide fabrication at the wafer-scale.

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Appendix A. Reduced order model of the laminated cantilever beams and effective mass

Following the theoretical model of [30], the equation of motion for a laminated cantilever beam of arbitrary cross section can be written:

$$m(x) \frac{\partial^2 u}{\partial t^2} + \frac{\partial^2}{\partial x^2} \left[D(x) \frac{\partial^2 u}{\partial x^2} \right] - \Theta V(t) \Delta(x) = p(x, t) \quad (A.1)$$

where $u(x, t)$ is the transverse displacement of the beam at axial position x and time t , $m(x)$ is the beam mass per unit of length, $D(x)$ is the beam bending stiffness, Θ is the piezoelectric transduction constant of the piezoelectric layer, proportional to d_{31} and e_{31} , $V(t)$ the applied voltage and:

$$\Delta(x) = -\frac{d}{dx} \delta(x - x_p) \quad (A.2)$$

where $\delta(x)$ is the Dirac function and x_p is the axial position of the piezoelectric layer end. The external mechanical force per unit of length is $p(x, t)$. Considering a given mode shape $\Phi(x)$, the associated modal mass is:

$$m_\Phi = \int_0^L m(x) \Phi^2(x) dx \quad (A.3)$$

Then, expanding $u(x, t)$ on the modal basis and truncating the result to a given mode shape $\Phi(x)$ only, one obtains:

$$u(x, t) = \Phi(x) r(t) \quad (A.4)$$

where the modal coordinate verifies:

$$\ddot{r} + Q^{-1} \omega_0 \dot{r} + \omega_0^2 r - \widetilde{\chi}_c V = \frac{1}{m_\Phi} \int_0^L p(x, t) \Phi(x) dx \quad (A.5)$$

where:

$$\widetilde{\chi}_c = \frac{\Theta}{m_\Phi} \frac{d\Phi}{dx}(x = x_p) \quad (A.6)$$

Considering that the tip displacement of the beam is $u_t = \Phi(L) r(t)$ and a uniform loading $p(x, t) = p_0(t)$, and introducing those expressions in (A.5), one obtains equation (1) with $\chi_c = \widetilde{\chi}_c \Phi(L)$. Using the finite element model of [29, 31] leads us to compute the integrals in m_Φ and M_1 with matrix products.

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